

Identifying an unknown function in a parabolic equation by Homotopy analysis method and comparison with the Adomian decomposition method

Abstract

In this paper, the homotopy analysis method is used for computing an unknown time-dependent parameter in an inverse quasilinear parabolic partial differential equation and compared with the Adomian decomposition method. To show the efficiency of the new approach, several test examples are presented.

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