

Normal Extensions of a Singular Differential Operator For First Order

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Abstract

In this work, in terms of boundary values all normal extensions of the minimal operator generated by a linear singular differential-operator expression for first order with operator coefficients in Hilbert space of vector-functions in a right half-infinite interval are described. Later on, a point spectrum of such extensions has been investigated.

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